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On the friction drag reduction mechanism of streamwise wall fluctuations

Tamás István Józsa^{a,*}, Elias Balaras^b, Maria Kashtalyan^c, Alistair George
Liam Borthwick^d, Ignazio Maria Viola^e

^a*Department of Engineering Science, Institute of Biomedical Engineering, University of
Oxford, Oxford OX1 3PJ, UK*

^b*Department of Mechanical and Aerospace Engineering, The George Washington
University, Washington, DC 20052, USA*

^c*School of Engineering, Centre for Micro- and Nanomechanics (CEMINACS), University of
Aberdeen, Aberdeen AB24 3UE, UK*

^d*School of Engineering, Institute for Infrastructure and Environment, University of
Edinburgh, Edinburgh EH9 3FB, UK*

^e*School of Engineering, Institute for Energy Systems, University of Edinburgh, Edinburgh
EH9 3FB, UK*

Abstract

Understanding how to decrease the friction drag exerted by a fluid on a solid surface is becoming increasingly important to address key societal challenges, such as decreasing the carbon footprint of transport. Well-established techniques are not yet available for friction drag reduction. Direct numerical simulation results obtained by Józsa *et al.* (2019) previously indicated that a passive compliant wall can decrease friction drag by sustaining the drag reduction mechanism of an active control strategy. The proposed compliant wall is driven by wall shear stress fluctuations and responds with streamwise wall velocity fluctuations. The present study aims to clarify the underlying physical mechanism enabling the drag reduction of these active and passive control techniques. Analysis of turbulence statistics and flow fields reveals that both compliant wall and active control amplify streamwise velocity streaks in the viscous sublayer. By doing so, these control methods counteract dominant spanwise vorticity fluctuations in the near-wall region. The lowered vorticity fluctuations lead to an overall weakening of vortical structures which then mitigates momentum transfer and

*Corresponding author

Email address: tamas.jozsa@eng.ox.ac.uk (Tamás István Józsa)

results in lower friction drag. These results might underpin the further development and practical implementation of these control strategies.

Keywords: Turbulent channel flow, Active flow control, Passive flow control, Drag reduction, Compliant wall, Compliant surface

2010 MSC: 76D55

1. Introduction

The question as to whether compliant walls can sustain drag reduction in turbulent flows has challenged fluid dynamicists in the decades [1] after Kramer’s somewhat controversial experiments [2–4]. The early research focus was on quantification of the impact of deformable surfaces on transitional flows. Studies based on linear stability analysis of flat plate boundary layers demonstrated that a pressure-driven surface can delay laminar-turbulent transition by damping Tollmien-Schlichting waves [5, 6]. It was reported that a wall made of compliant panels could postpone natural transition indefinitely [7], and such transition delay was confirmed for in-plane channel flows [8]. Sixty years after Kramer’s experiments, this phenomenon is now widely accepted owing to carefully conducted experiments [9–11] and numerical investigations [12, 13].

Later research studies have aimed to characterise the interaction of compliant surfaces and fully-developed turbulent flows. Theoretical [14] and experimental [15–17] studies suggested that travelling wave-like surface deformations could suppress turbulence production in turbulent boundary layers. Conversely, studies based on Direct Numerical Simulations (DNS) [18–22] and resolvent analysis [23, 24] reported minimal changes or increased friction drag in the presence of compliant surfaces. The results implied that pressure-driven wall-normal deformations cannot utilise the drag reduction mechanisms of opposition control [25–28] and streamwise-travelling waves [29] at low Reynolds numbers.

To date, experimental work has mostly targeted single-layer isotropic viscoelastic materials that exhibit primarily wall-normal deformations [9–11, 15–17, 30–32]. By comparison, the majority of computational studies solely ex-

25 aminated pressure-driven compliant walls represented by dynamic systems with
 26 wall-normal displacement response [18, 20, 33]. Only a few studies have con-
 27 sidered the effects of passive in-plane wall motions [19, 34–36]. Furthermore,
 28 computational studies on flow control have been restricted to low Reynolds
 29 numbers with few exceptions, such as [37].

30 Recently, it has been demonstrated by means of DNS that even small-scale
 31 spanwise deformations can act like a wall with spanwise slip [38] and result in
 32 substantial drag penalty [34]. The latter study also reported that a conceptual
 33 compliant wall can imitate streamwise active flow control originally proposed by
 34 [25]. Importantly, it was found that drag reduction is sustained by streamwise
 35 wall fluctuations driven by streamwise wall shear stress fluctuations.

36 The present study aims to examine the drag reduction mechanism of active
 37 and passive flow control techniques with streamwise wall velocity responses at
 38 low and moderate Reynolds numbers for the first time. To this end, a database
 39 of controlled and uncontrolled canonical turbulent channel flows at low and
 40 moderate friction Reynolds numbers ($Re_\tau \approx 180$ and 1000) is analysed and
 41 extended with flow visualisations, Reynolds stress transport statistics and La-
 42 grangian wall motion tracking [39]. The paper is structured as follows. Section
 43 2 outlines the computational methodology. Section 3 presents the main results
 44 for active and passive control methods in terms of integral variables, the fluc-
 45 tuating flow field, turbulence statistics, and Lagrangian wall motions. Section
 46 4 lists the main findings. It should be noted that preliminary results were pre-
 47 sented at the Eleventh International Symposium on Turbulence and Shear Flow
 48 Phenomena (TSFP11) [40].

49 **2. Methods**

50 *2.1. Simulation Settings*

51 Herein, fully-developed turbulent flow in an idealised plane channel is mod-
 52 elled by the incompressible continuity and Navier-Stokes momentum equations
 53 (see e.g. [41]), which are discretised on a Cartesian staggered grid and solved

Table 1: Simulation settings. L_1 , L_2 , and L_3 are the streamwise, wall-normal and spanwise lengths of the computational domain, and n_1 , n_2 , and n_3 are the corresponding grid resolutions. Δt denotes the time step, whereas t_a is the averaging time.

| Case | low Re | moderate Re |
|--|-------------------------------|------------------------------|
| Reynolds number, Re | 2857 | 20000 |
| friction Reynolds number, Re_τ | 180.7 (≈ 180) | 990.2 (≈ 1000) |
| domain size, $L_1 \times L_2 \times L_3$ | $4\pi \times 2 \times 4\pi/3$ | $2\pi \times 2 \times \pi$ |
| number of nodes, $n_1 \times n_2 \times n_3$ | $290 \times 251 \times 290$ | $770 \times 1001 \times 770$ |
| temporal resolution, $\Delta t u_\tau^2 / \nu$ | ≈ 0.115 | ≈ 0.196 |
| averaging time, $t_a u_\tau^2 / \nu$ | ≈ 23000 | ≈ 19600 |

numerically by an in-house fractional step solver [42]. Spatial derivatives are represented by second-order central-differences. The pressure-Poisson equation is solved directly [43] using fast Fourier transforms in the periodic (streamwise and spanwise) directions, and by a standard tridiagonal matrix algorithm [44] in the wall-normal direction. For time integration, an explicit third-order low-storage Runge-Kutta method is utilised for the streamwise and spanwise momentum equations, whereas the implicit Crank-Nicolson scheme is used for the wall-normal momentum equation. A detailed description of the in-house incompressible Navier-Stokes solver is given by [45].

We denote the streamwise, wall-normal, and spanwise Cartesian coordinates in the channel as x_1 , x_2 , x_3 , and the corresponding velocity and vorticity components as u_1 , u_2 , u_3 , and ω_1 , ω_2 , ω_3 . Non-dimensional quantities are based on the channel half-height δ and bulk velocity u_b . The (bulk velocity) Reynolds number is defined as $Re = u_b \delta / \nu$, where ν denotes kinematic viscosity. Quantities with + superscripts are non-dimensionalised with respect to the friction velocity $u_\tau = \sqrt{\langle \tau_1 \rangle} / \rho$ and the viscous length scale $\delta_\nu = \nu / u_\tau$ of the baseline (uncontrolled) simulations. The friction Reynolds number is defined as $Re_\tau = u_\tau \delta / \nu$. Here, ρ is the fluid density and τ_1 is the streamwise wall shear stress component. The angled brackets $\langle \rangle$ indicate an averaged variable and the prime symbol ' denotes a fluctuating quantity. Table 1 lists the basic simulation settings. For further details of the model and its verification and validation tests, the reader is referred to [34, 39].

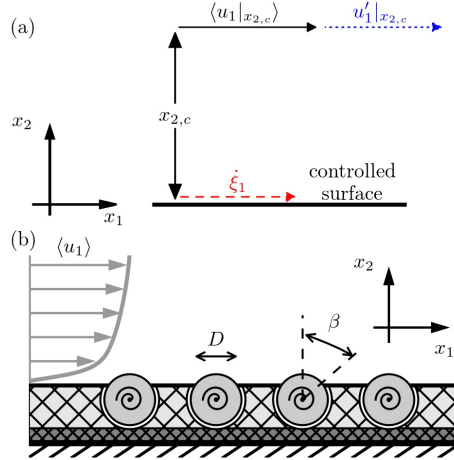


Figure 1: Schematic drawing of the implemented flow control techniques introducing stream-wise wall fluctuations: (a) active control based on Eq. (1); (b) a compliant wall model including mounted rotating discs with spanwise aligned axes. The compliant wall is modelled using Eq. (2). These figures are modified with permission from Józsa *et al.* [34].

2.2. Boundary Conditions

The streamwise (x_1) and spanwise (x_3) directions are by definition periodic. In the uncontrolled (baseline) simulations, the channel walls (bounding x_1 - x_3 planes) are hydrodynamically smooth no-slip walls. The active flow control and the compliant wall impose two different Dirichlet boundary conditions for the streamwise wall velocity component at both channel walls. The other two velocity components and the wall-normal pressure gradient at the channel walls are set to zero. Figure 1(a) shows the active flow control introduced in [25], where the fluctuating streamwise fluid velocity is measured at $x_{2,c}$ distance from the wall ($u'_1|_{x_{2,c}}$, sensing), and the wall velocity directly below the measurement location is equal to the measured streamwise velocity fluctuation both in direction and magnitude ($\dot{\xi}_1 = u_1|_{\text{wall}}$, actuation). Based on figure 1(a), the active flow control is implemented as

$$\dot{\xi}_1 = u'_1|_{x_{2,c}} = u_1|_{x_{2,c}} - \langle u_1|_{x_{2,c}} \rangle. \quad (1)$$

The compliant wall case exploits a drag reduction mechanism similar to that of active flow control, with streamwise wall shear stress component (τ_1) as input

and streamwise wall velocity components ($u_{1,\text{wall}}$) as output [34, 39, 40]. Figure 1(b) shows a conceptual model of such a compliant surface utilising mounted discs, inspired by a former active control study [46]. These discs have finite spanwise extent that is comparable to the viscous length scale (δ_ν). Therefore, the wall velocity response of the compliant surface exhibits streamwise and spanwise variations which are required for a successful control, as demonstrated in Sections 3.2 and 3.4. With sufficiently small disc diameter (D) and β angle (e.g. $D \sim \delta_\nu$ and $\beta < \pi/6$), a simplified dimensionless governing equation of the compliant wall can be written as

$$\underbrace{\frac{4C_m}{D^2 A_s}}_{\Lambda_m} \ddot{\xi}_1 + \underbrace{\frac{4C_d}{D^2 A_s}}_{\Lambda_d} \dot{\xi}_1 + \underbrace{\frac{4C_s}{D^2 A_s}}_{\Lambda_s} \xi_1 = \frac{1}{Re} \frac{\partial u_1}{\partial x_2} \Big|_{\text{wall}}, \quad (2)$$

assuming that the motion of the discs is driven by the local wall shear stress. Here, Λ_m , Λ_d and Λ_s are the inertia, damping, and spring stiffness parameters of the compliant surfaces, respectively. These parameters are proportional to the moment of inertia (C_m), viscous damping (C_d), and torsion spring coefficient (C_s) of a single mounted disc, and inversely proportional to its wetted surface area (A_s). In Eq. (2), ξ_1 is the tangential displacement of a disc. The resulting tangential velocity is assumed to be equivalent to the introduced streamwise wall velocity ($\dot{\xi}_1 = u_{1,\text{wall}}$). If the β angle shown in Figure 1(b) is less than 30° , then this approximation leads to less than 5% error in the streamwise wall velocity compared to the exact formulation which accounts for the Cartesian velocity distribution over the disc surface [39]. Considering that the surface integral of the wall-normal velocities over the wetted surface is zero, the disc diameter is restricted so that the impact of the introduced wall-normal velocity is negligible.

During compliant wall simulations, Eq. (2) is imposed at every wall cell. To advance Eq. (2) in time, a fourth order Runge-Kutta scheme is employed, and a weak coupling scheme is implemented to treat the resulting fluid-structure interaction problem. The governing equation of the compliant surface ensures

120 that the average streamwise wall velocity remains zero ($\langle u_1 \rangle = 0$) because the
 121 average displacement of the discs balances the average streamwise wall shear
 122 stress.

123 *2.3. Measuring Control Effects*

124 To keep the volumetric flow rate constant, the driving pressure gradient
 125 ($\partial P / \partial x_1$) is adjusted at every time step. With this in mind, the Drag Reduction
 126 (DR) in the case of controlled simulations is defined as

$$127 \quad \text{DR} = 1 - \frac{\langle \partial P / \partial x_1 \rangle_{\text{controlled}}}{\langle \partial P / \partial x_1 \rangle_{\text{baseline}}}. \quad (3)$$

128 In addition, the following global (integral) variables are introduced to quantify
 129 the effects of the control methods on the entire flow field [47]. Using the Einstein
 130 summation convention, the global turbulent kinetic energy is defined as

$$131 \quad k_g = \frac{1}{\delta} \int_0^\delta k dx_2 = \frac{1}{\delta} \int_0^\delta \frac{\langle u'_i u'_i \rangle}{2} dx_2. \quad (4)$$

132 Similarly, the global turbulent enstrophy is computed from the fluctuating vor-
 133 ticity components as

$$134 \quad \mathcal{E}_g = \frac{1}{\delta} \int_0^\delta \mathcal{E} dx_2 = \frac{1}{\delta} \int_0^\delta \langle \omega'_i \omega'_i \rangle dx_2. \quad (5)$$

135 Furthermore, the absolute change (Δ) and the relative change (Δ_r) of a general
 136 quantity (q) are defined as

$$137 \quad \Delta q = q_{\text{controlled}} - q_{\text{baseline}}, \quad (6)$$

138 and

$$139 \quad \Delta_r q = \frac{q_{\text{controlled}} - q_{\text{baseline}}}{q_{\text{baseline}}}. \quad (7)$$

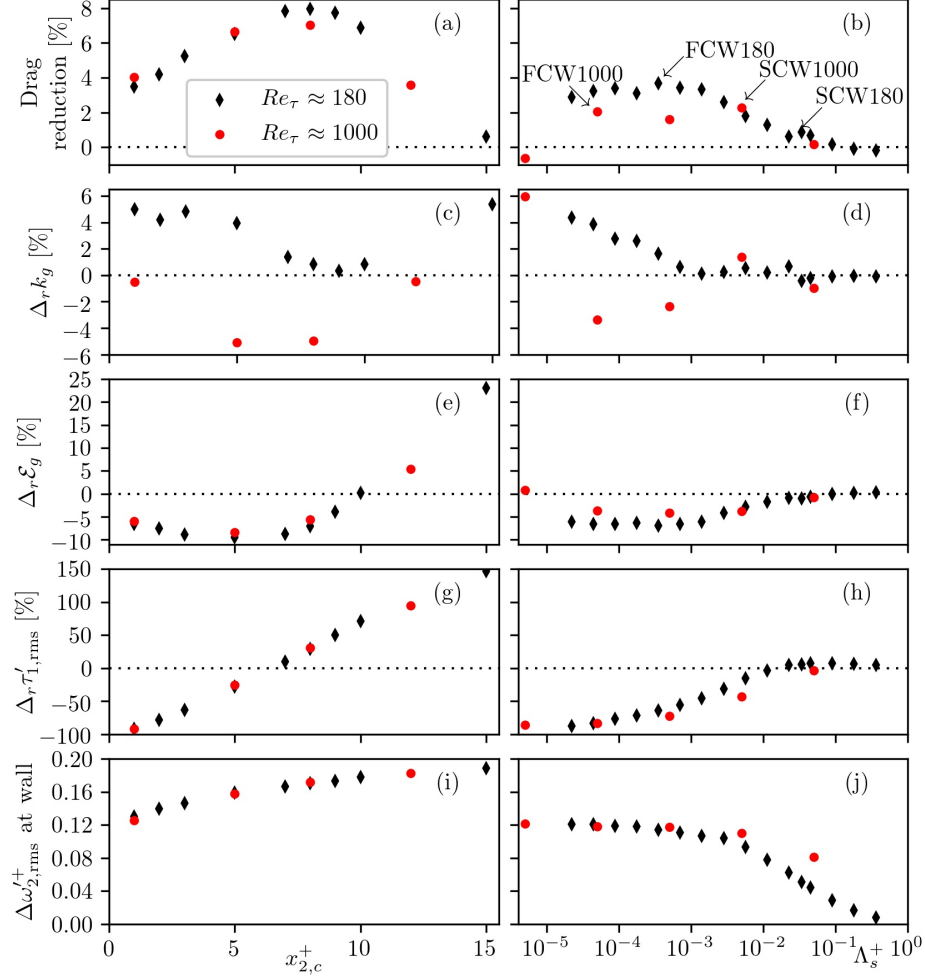


Figure 2: Effects of the active and passive control techniques on drag reduction (a)-(b), relative change in global turbulent kinetic energy (c)-(d), relative change in global turbulent enstrophy (e)-(f), relative change in rms streamwise wall shear stress fluctuations (g)-(h), and absolute change in rms wall-normal vorticity fluctuations at the wall (i)-(j), as functions of control distance (left column) and spring parameter (right column), respectively. The dotted lines indicate the zero level.

3. Results and Discussion

3.1. Integral variables

Figure 2 shows the effect of different control cases on certain integral variables listed in Section 2.3. From Figures 2(a) and (g), it can be seen that the Active Flow Control (AFC) with $x_{2,c}^+ = 1$ leads to ca. 4% drag reduction accompanied with a more than 90% drop in the root-mean-square (rms) streamwise wall shear stress fluctuations $\tau'_{1,\text{rms}}$ at $Re_\tau \approx 180$ and 1000. Maximum drag reductions of 8% and 7% at $Re_\tau \approx 180$ and 1000 respectively are attained for active control with $x_{2,c}^+ = 8$. Active control also performs well when the global turbulent enstrophy is decreased, as indicated in Figure 2(e). However, it is somewhat counter-intuitive that (i) maximum drag reduction occurs when there is a 30% increase in $\tau'_{1,\text{rms}}$; and (ii) drag reduction is accompanied by an increase in global turbulent kinetic energy at $Re_\tau \approx 180$. This behaviour can be observed in Figures 2(a), (c), and (g). From Figure 2(g), it can be concluded that active control can have fluctuating shear-cancelling and shear-increasing modes corresponding to decreased ($\Delta_r \tau'_{1,\text{rms}} < 0$) and increased ($\Delta_r \tau'_{1,\text{rms}} > 0$) streamwise wall shear stress fluctuations, respectively. Both modes are tied to an increase in wall-normal vorticity fluctuations as shown in Figure 2(i). Sections 3.2 and 3.3 aim to explain these observations based on analyses of the flow fields and turbulence statistics, respectively.

The three-dimensional parameter space of the compliant wall is mapped using a semi-analytical method, following [34, 35]. Using the resulting framework, we optimise parameters for maximal $\tau'_{1,\text{rms}}$, noting that active control provides maximum drag reduction when in a shear-increasing mode [39]. DNS at $Re_\tau \approx 180$ reveals that the resulting parameter set corresponds to a Stiff Compliant Wall (SCW180), increases $\tau'_{1,\text{rms}}$ by ca. 6%, and has a marginal impact on friction drag (see Table 2). Taking SCW180 as the starting point, a parameter sweep is performed by changing solely the spring parameter for simplicity, as shown in Figure 2. The results presented in Figure 2(h) confirm that compliant walls sustaining streamwise velocity fluctuations have shear-

170 cancelling ($\Delta_r \tau'_{1,\text{rms}} < 0$) and shear-increasing ($\Delta_r \tau'_{1,\text{rms}} > 0$) modes, similar
 171 to active control. Figure 2(b) shows a Flexible Compliant Wall (FCW180) cor-
 172 responding to peak drag reduction measured in the present study (see Table
 173 2). FCW180 results in 3.68% drag reduction at $Re_\tau \approx 180$ which is more than
 174 twice the maximum value reported by other computational studies on compli-
 175 ant surfaces (1.7%) [20]. Considering other passive control techniques, the peak
 176 drag reduction is lower than the value measured with riblets ($\approx 8\%$) [48–50]
 177 but higher than the value measured with wavy walls (0.6%) [51]. FCW180 has
 178 been tested for modified domain sizes, spatial and temporal resolutions, and
 179 sample sizes, and a thorough error quantification found a $\pm 1\%$ uncertainty in
 180 drag reduction [34]. The domain size has been identified as the primary error
 181 source. Therefore $\pm 1\%$ drag reduction uncertainty is representative of the low
 182 Reynolds number cases but simulations at $Re_\tau \approx 1000$ suffer from a somewhat
 183 larger uncertainty. Detailed uncertainty quantification for the $Re_\tau \approx 1000$ case
 184 is an outstanding challenge because simulations at moderate Reynolds numbers,
 185 especially with increased domain size, are extremely resource intensive

Table 2: Parameters of selected compliant walls (SCW180, FCW180, etc.) and corresponding drag reduction (DR).

| ID | $Re_\tau \approx$ | Λ_m | Λ_d | Λ_s | DR [%] |
|---------|-------------------|----------------------|-------------|----------------------|--------------|
| SCW180 | 180 | $1.40 \cdot 10^{-3}$ | 0 | $3.38 \cdot 10^{-2}$ | 0.86 |
| FCW180 | 180 | $1.40 \cdot 10^{-3}$ | 0 | $3.50 \cdot 10^{-4}$ | 3.68 ± 1 |
| SCW1000 | 1000 | $4.00 \cdot 10^{-4}$ | 0 | $5.00 \cdot 10^{-3}$ | 2.29 |
| FCW1000 | 1000 | $4.00 \cdot 10^{-4}$ | 0 | $5.00 \cdot 10^{-5}$ | 2.04 |

186 Simulations are carried out at $Re_\tau \approx 1000$ to gain insight into the effect
 187 of increasing Reynolds number (Table 2 and Figure 2). The inertia param-
 188 eter, Λ_m is decreased for these simulations to ensure that compliant surfaces
 189 remain responsive. The investigated parameters lead to significant performance
 190 degradation with increasing Reynolds number but both FCW180 and FCW1000
 191 sustain a considerable decrease in $\tau'_{1,\text{rms}}$ accompanied with drag reduction. Ac-
 192 cording to Figure 2(b), the drag reduction curve breaks down with decreasing
 193 spring parameter. Hence, $\tau'_{1,\text{rms}} = 0$ is not optimal for passive control. We

find that stiffer compliant walls can perform better at $Re_\tau \approx 1000$ compared to $Re_\tau \approx 180$ (see SCW180 and SCW1000 in Table 2 and Figure 2(b)). Although, the impacts of the other parameters (Λ_m and Λ_d) at $Re_\tau \approx 180$ have been reported in our previous studies [34, 39], the parameter space at $Re_\tau \approx 1000$ remains mostly unexplored because of the associated high computational cost.

Pairwise comparisons between Figures 2 (g)-(h) and (i)-(j) suggest that as $\Lambda_s \rightarrow 0$, the effect of passive control on wall quantities approaches that of active control with $x_{2,c}^+ = 1$. The source of this similarity is determined through manipulation of the control equations. Substituting a Taylor series expansion of u_1' near the wall into Equation (1) leads to

$$\left. \frac{\partial u_1'}{\partial x_2} \right|_{\text{wall}} x_{2,c} + \frac{1}{2} \left. \frac{\partial^2 u_1'}{\partial x_2^2} \right|_{\text{wall}} x_{2,c}^2 + \mathcal{O}(x_{2,c}^3) = 0. \quad (8)$$

This equation suggests that if the control distance is small ($x_{2,c}^+ = 1$) then the active control cancels the spanwise vorticity fluctuations at the wall:

$$\omega'_{3,\text{wall}} = - \left. \frac{\partial u_1'}{\partial x_2} \right|_{\text{wall}} = - \frac{\tau_1'}{\rho\nu} = 0. \quad (9)$$

With respect to passive control, Equation (2) tends to Equation (9) as the control parameters tend to zero ($\Lambda_m \rightarrow 0$, $\Lambda_d \rightarrow 0$, and $\Lambda_s \rightarrow 0$, leading to $\tau_1' \rightarrow 0$). This prediction regarding the asymptotic behaviour of the passive control overlaps with the result of parameter space mapping reported in [34, 39].

3.2. Fluctuating Flow Field Analysis

Both the active and passive control methods interact primarily with the so called near-wall cycle that comprises quasi-streamwise vortices and streamwise velocity streaks driven by the mean shear [52]. Figure 3 illustrates the three-dimensional arrangement of typical instantaneous vortical features, including a hairpin vortex formation [53] and the connected counter-rotating vortices [52, 54]. The streamwise control techniques do not noticeably modify these vortical features [39]. Visualisation of the vorticity field offers an alternative method by which to detect qualitative changes in the flow field, and has been proven to be

221 an efficient means to understand flow control [55]. Here, the vorticity field is
 222 explored by seeding vorticity lines of the instantaneous fluctuating flow field as
 223 visualised in Figure 3. In Figure 3, the high and low momentum regions (streaks)
 224 corresponding to the vortical features are represented by the fluctuating vorticity
 225 lines. Within the streaks, where streamwise fluctuations and the corresponding
 226 shear dominate, fluctuating vorticity lines (ω' lines) form a spiral shape with
 227 quasi-streamwise aligned axis.

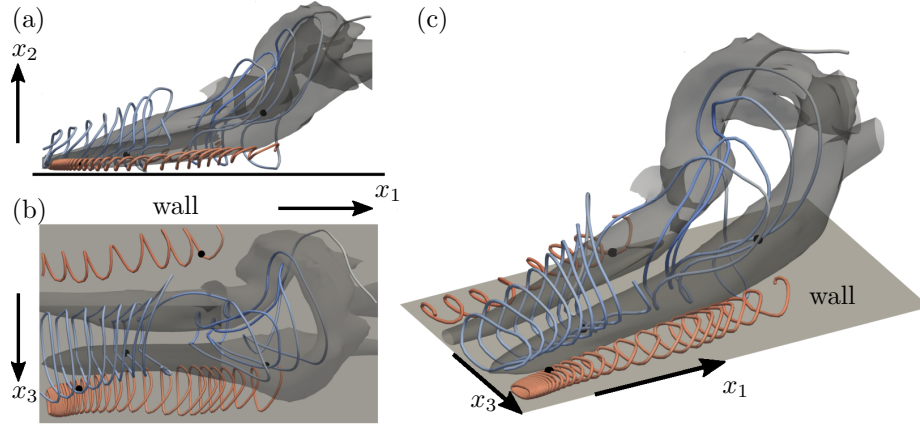


Figure 3: Instantaneous flow features near the wall at $Re_\tau \approx 1000$: (a) side view; (b) top view; (c) bird's eye view. The total wall-normal extent of the $Q = 35$ isosurface [56] is about $100\delta_\nu$. The streamwise and spanwise extent of the presented wall section is $190\delta_\nu$, and $110\delta_\nu$, respectively. The black spheres indicate fluctuating vorticity line seeding points. A hairpin vortex is formed around the blue fluctuating vorticity lines enclosed by a low momentum region. The remaining two red vorticity lines are enclosed by high momentum regions.

228 We now summarise the key kinematic properties of fluctuating vorticity lines
 229 with increasing wall distance based on Figure 3 and baseline velocity and vor-
 230 ticity statistics given in Appendix A. First, $\omega'_3 \gg \omega'_1 > \omega'_2$, and hence ω' lines
 231 lie parallel to the x_1 - x_3 plane. Near the wall, $\omega'_3 \approx -\partial u'_1 / \partial x_2 \propto \tau'_1$ represents
 232 flow shear between the streaks and the wall. Fluctuating vorticity lines are di-
 233 rected towards the wall-normal direction between the low- and high-momentum
 234 streaks, highlighting that $\omega'_2 \approx -\partial u'_1 / \partial x_3$. In the buffer layer, streak instabil-
 235 ities emerge [52] as the viscous force weakens. The streamwise vorticity (ω'_1)
 236 exhibits a statistical local maximum at about $x_2^+ = 20$, corresponding to the
 237 mean wall distance of the centre-line of quasi-streamwise vortices. If $x_2^+ \ll 20$,

238 then $\omega'_1 \approx \partial u'_3 / \partial x_2 \propto \tau'_3$ gives a measure of shear between the wall and quasi-
 239 streamwise vortices. For $x_2^+ > 50$, vorticity fluctuations, unlike velocity fluctu-
 240 ations, are approximately isotropic [54], i.e. $\langle \omega'_1 \omega'_1 \rangle \approx \langle \omega'_2 \omega'_2 \rangle \approx \langle \omega'_3 \omega'_3 \rangle$. Above
 241 $x_2^+ \approx 100$, hairpin vortices can be detected by the Q -criterion or vorticity line
 242 bundles but vorticity lines are mostly disorganised [57, 58]. At the Reynolds
 243 numbers investigated in this study, fluctuating vorticity lines remain rooted in
 244 the viscous sublayer suggesting that the entire flow field is attached to the wall
 245 and can be modified by wall motions.

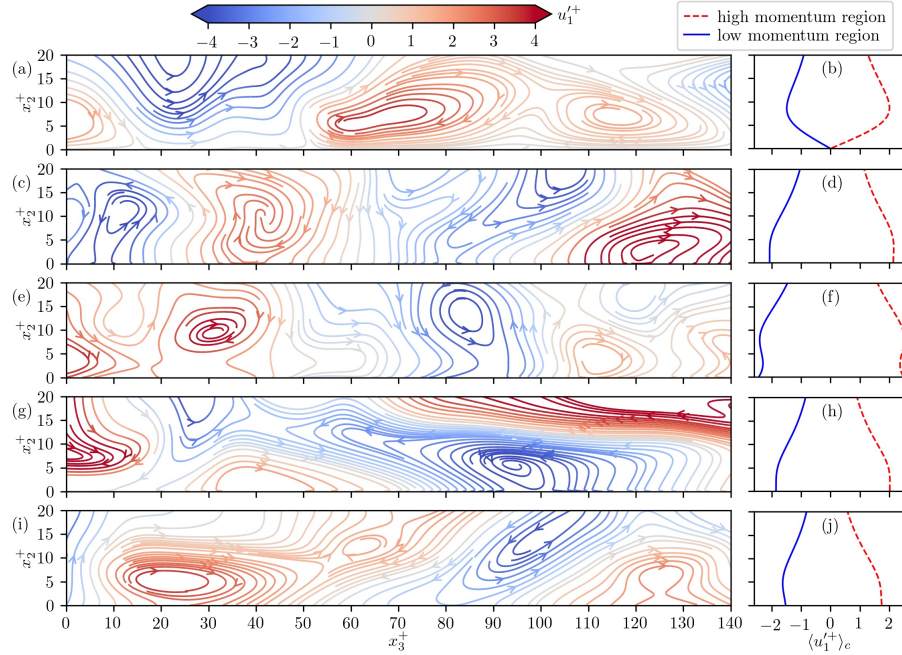


Figure 4: Effects of active and passive control techniques on instantaneous near-wall ω' lines (left column) and $\langle u'_1 \rangle_c$ profiles (right column) at $Re_\tau \approx 1000$. The ω' lines are visualised along a cross-section and are coloured by u'_1 . Baseline case (a)-(b), active control with $x_{2,c}^+ = 1$ (c)-(d), active control with $x_{2,c}^+ = 8$ (e)-(f), FCW1000 (g)-(h), SCW1000 (i)-(j). Similar trends can be observed at $Re_\tau \approx 180$.

246 Next, these vorticity features are investigated in the controlled channels, as
 247 depicted in the left column of Figure 4. In addition, conditionally averaged
 248 streamwise velocity profiles ($\langle u'_1 \rangle_c$) of the low and high momentum regions are
 249 presented in the right column of Figure 4. These regions are distinguished ac-

250 cording to the sign of the streamwise wall shear stress fluctuations and the sign
 251 of the wall velocity fluctuations in the baseline and controlled cases, respectively.
 252 The left column of Figure 4 suggests that the walls become part of the stream-
 253 wise velocity streaks as a result of the control. The ω' lines highlight a twofold
 254 impact on the near-wall vorticity fluctuations: (i) spanwise vorticity fluctua-
 255 tions are suppressed; and (ii) wall-normal vorticity fluctuations are introduced.
 256 The flattened velocity profiles in the right column of Figure 4 confirm span-
 257 wise vorticity cancellation in the case of actively and passively controlled walls.
 258 The streaky wall motions promoted by the control methods induce wall-normal
 259 vorticity at the wall, as shown in Figures 2(i)-(j). The increased wall-normal
 260 vorticity component ω_2 relates to enhanced shear-layers between low- and high-
 261 momentum streaks (see Figure 4(c), (e), (g), and (i)).

262 In shear-increasing mode, active control amplifies ω'_3 very close to the wall
 263 because of reversed shear, as depicted in Figure 4(f). This behaviour can be
 264 deduced from the second order approximation of the active control equation:

$$\left. \frac{\partial u'_1}{\partial x_2} \right|_{\text{wall}} > 0 \text{ if } \left. \frac{\partial^2 u'_1}{\partial x_2^2} \right|_{\text{wall}} < 0, \quad (10)$$

266 and *vice versa*. Therefore, active control naturally creates a velocity profile
 267 with reversed shear as $x_{2,c}$ increases. Active control attains peak performance
 268 by reversing fluctuating shear at the wall, and thus cancelling the dominant
 269 spanwise vorticity fluctuations. Sustaining such states requires energy input
 270 and hence it is not possible with a passive compliant surface [34].

271 It appears that a decrease in net vorticity fluctuations at the wall damps
 272 vorticity fluctuations throughout the boundary layer, and mitigates momentum
 273 transfer which in turn contributes to turbulent friction drag. Wall motions
 274 induced by the control techniques lower spanwise vorticity fluctuations by de-
 275 creasing the shear between wall and streaks; this process inevitably increases
 276 shear between the streaks. Amplified shear between the streaks manifests itself
 277 as increased wall-normal vorticity in the near-wall region (shown in Figures 2(i)
 278 and (j)), which is undesirable according to the above hypothesis. Consequently,

streamwise control has simultaneously positive and negative effects which limit the control performance and cause the corresponding drag reduction curve to break down.

In summary, streamwise wall motions dictated by the control methods can reduce spanwise vorticity fluctuations (i.e. shear between the streaks and wall) but increasingly build up undesirable wall-normal vorticity fluctuations (i.e shear between the streaks) by doing so. For this reason, streamwise wall fluctuations can weaken turbulence when ω'_3 cancellation dominates over ω'_2 amplification but such wall motions cannot relaminarise the flow. In this sense, this drag reduction mechanism is unique. By comparison, wall-normal and spanwise opposition control [25–28] and spanwise wall oscillations [37, 59, 60] increase near-wall vorticity fluctuations to counteract quasi-streamwise vortices and weaken the near-wall cycle (which is known to be a major contributor to turbulence production).

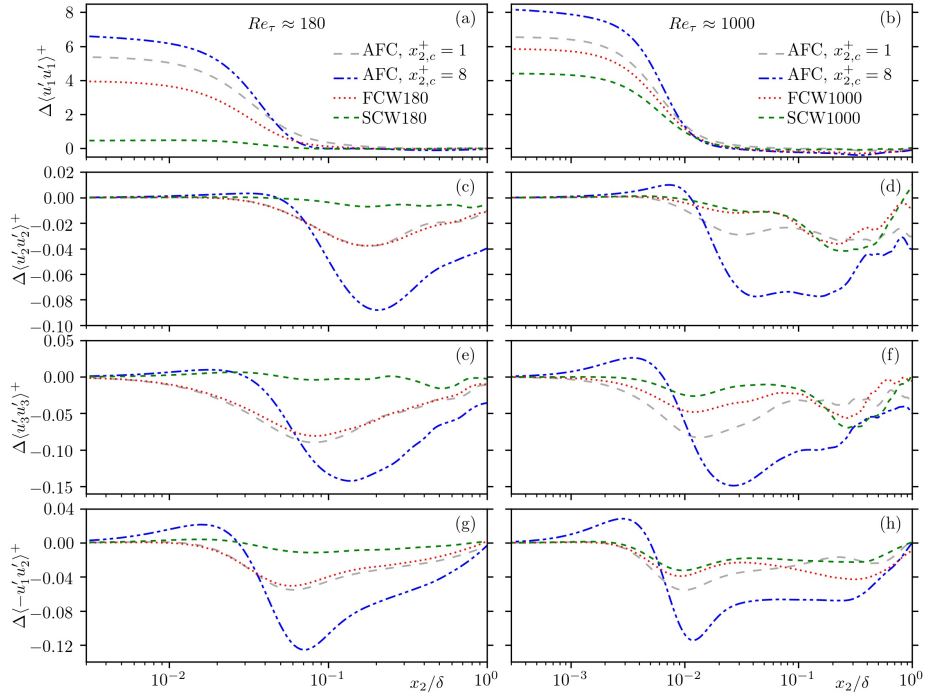


Figure 5: Change in Reynolds stresses with wall distance for different control techniques at $Re_\tau \approx 180$ (left column) and at $Re_\tau \approx 1000$ (right column). Streamwise (a)-(b), wall-normal (c)-(d), spanwise (e)-(f) components, and Reynolds shear stress (g)-(h).

3.3. Turbulence Statistics

To investigate the drag reduction mechanism, we examine how the control methods modify turbulence statistics in comparison to baseline values available in [Appendix A](#). The control techniques cause qualitative changes only in the most energetic streamwise velocity fluctuations characterised by $\langle u'_1 u'_1 \rangle$. Figures 5(a) and (b) indicate that the control methods amplify streamwise velocity streaks by inducing significant streamwise fluctuations in the near-wall region. In exchange, a slight drop in the remaining Reynolds stress components is evident from Figures 5(c)-(h). According to Figure 5(a), the global turbulent kinetic energy at $Re_\tau \approx 180$ is increased (Figure 2(c)-(d)) when the control methods are applied because the amplified streaks fill about 10% of the channel. At $Re_\tau \approx 1000$, the control techniques energise the streaks similarly, but with increasing Reynolds number the wall-normal extent of the streaks reduces. Based on Figure 5(b), near-wall streaks occupy only ca. 2% of the channel at $Re_\tau \approx 1000$. In addition, at $Re_\tau \approx 1000$, the control methods weaken the large-scale motions of the log-layer, which contain most of the turbulent kinetic energy at high Reynolds numbers [61, 62]. This phenomenon can be observed in Figure 5(b), where $\Delta\langle u'_1 u'_1 \rangle$ is negative above $x/\delta = 0.05$. The increase in $\langle u'_1 u'_1 \rangle$ in Figure 5(a)-(b), and decreases in $\langle u'_2 u'_2 \rangle$, $\langle u'_3 u'_3 \rangle$, and $\langle -u'_1 u'_2 \rangle$ visible in Figure 5(c)-(h) suggest that momentum transfer decreases between the streamwise and other velocity components compared to the baseline case.

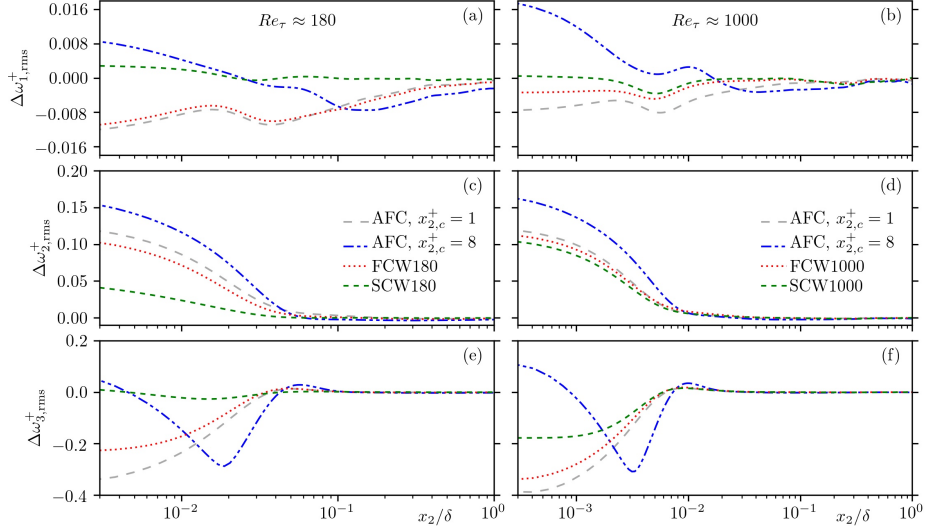


Figure 6: Change in root-mean-square fluctuating vorticity components with wall distance for different control techniques at $Re_\tau \approx 180$ (left column) and at $Re_\tau \approx 1000$ (right column). Streamwise (a)-(b), wall-normal (c)-(d), and spanwise (e)-(f) components.

313 The streamwise wall motions of the control methods directly modify the
314 spanwise vorticity fluctuations depicted in Figure 4. Figure 6(e)-(f) shows un-
315 equivocally the strong influence of the control techniques on the spanwise vor-
316 ticity fluctuations (and therefore on streamwise wall shear stress fluctuations),
317 especially in the near-wall region. The rms spanwise vorticity profiles underline
318 that the active control in shear-cancelling mode ($x_{2,c}^+ = 1$) and efficient compli-
319 ant walls, such as FCW180, FCW1000, and SCW1000, damp spanwise vorticity
320 fluctuations at the wall. In shear-increasing mode, the active control amplifies
321 ω'_3 very close to the wall. However, as depicted by the lines corresponding to
322 $x_{2,c}^+ = 8$ in Figures 6(e) and (f), the increase in ω'_3 at the wall turns into a net
323 cancellation of ω'_3 in the near-wall region. This behaviour is a direct consequence
324 of the fluctuating velocity profiles with reversed shear, as visualised in Figure
325 4(f).

326 The rms wall-normal vorticity profiles (ω'_2) in Figures 6(c)-(d) confirm that
327 the control methods introduce statistically significant wall-normal vorticity fluc-
328 tuations representing increased shear between the streaks. Whereas FCW180,

329 FCW1000 and the active control with $x_{2,c}^+ = 1$ lower ω'_1 throughout the do-
 330 main, streamwise vorticity fluctuations are amplified in the vicinity of the wall
 331 in the case of active control with $x_{2,c}^+ = 8$ and SCW180 and SCW1000 according
 332 to Figures 6(a)-(b). In every case where statistically significant drag reduction
 333 (more than 1%) occurs, vorticity fluctuations are increased only in the near-wall
 334 regions, which account for 10% and 2% of the channels, at $\text{Re}_\tau \approx 180$ and 1000,
 335 respectively. Figures 6(a)-(d) and Figures 6(e)-(f) reveal that successful control
 336 methods weaken vorticity fluctuations throughout the majority of the channel
 337 compared to the baseline case, owing to spanwise vorticity cancellation near the
 338 wall.

339 The near-wall cycle contributes significantly to turbulence production in
 340 boundary layers [52]. Nonlinear interactions between the mean flow, quasi-
 341 streamwise vortices, and velocity streaks redistribute near-wall streamwise mo-
 342 mentum fluctuations first to spanwise and then to wall-normal momentum
 343 fluctuations as the wall distance increases [54]. The negative regime of the
 344 $\Delta_r \omega'_{1,\text{rms}}$ curves in Figures 6(a)-(b) implies that quasi-streamwise vortices are
 345 weakened by the control. For this reason, a lower turbulence production and
 346 inter-component momentum transfer compared to the baseline case should be
 347 measurable based on the Reynolds stress budgets.

348 The Reynolds stress transport equation [41, 63] for statistically steady state
 349 turbulent flows reads as

$$\langle u_k \rangle \frac{\partial \langle u'_i u'_j \rangle}{\partial x_k} = P_{ij} + T_{ij} + \Pi_{ij} + D_{ij} + \epsilon_{ij}. \quad (11)$$

351 where P_{ij} is the production rate, T_{ij} is the turbulent transport rate, Π_{ij} denotes
 352 the velocity-pressure gradient term, D_{ij} is the viscous diffusion rate, and ϵ_{ij} is
 353 the dissipation rate of the corresponding Reynolds stress components. Expand-

ing these terms from the right hand side of Eq. (11) leads to

$$\begin{aligned}
P_{ij} &= -\langle u'_i u'_k \rangle \frac{\partial \langle u_j \rangle}{\partial x_k} - \langle u'_j u'_k \rangle \frac{\partial \langle u_i \rangle}{\partial x_k}; \\
T_{ij} &= -\frac{\partial \langle u'_i u'_j u'_k \rangle}{\partial x_k}; \\
\Pi_{ij} &= -\left\langle u'_i \frac{\partial p'}{\partial x_j} \right\rangle - \left\langle u'_j \frac{\partial p'}{\partial x_i} \right\rangle; \\
D_{ij} &= \frac{1}{\text{Re}} \frac{\partial^2 \langle u'_i u'_j \rangle}{\partial x_k \partial x_k} \text{ and} \\
\epsilon_{ij} &= -\frac{2}{\text{Re}} \left\langle \frac{\partial u'_i}{\partial x_k} \frac{\partial u'_j}{\partial x_k} \right\rangle.
\end{aligned} \tag{12}$$

Thereafter, turbulent kinetic energy transport terms can be computed based on Equations (4) and (11) so that, for instance, $P_k = P_{ii}/2$.

Baseline turbulent kinetic energy and Reynolds shear stress budgets are listed in Appendix B. Regarding near-wall turbulent kinetic energy transport, the control techniques cause the most distinct increase in dissipation (less loss) balanced by diffusion (D) as shown in Figures 7(a) and (b). Global turbulent kinetic energy dissipation is linked to global enstrophy [47], and hence the control techniques weaken dissipation (the leading loss term of turbulent kinetic energy) by reducing vorticity fluctuations. Weakened turbulent dissipation is naturally accompanied by amplified near-wall (mainly streamwise) fluctuations.

The sum of the velocity-pressure gradient term and the turbulent transport rate ($\Pi_{ij} + T_{ij}$) dictates momentum distribution between the diagonal Reynolds stress components [63]. From Figures 7(a) and (b), decreased $\Pi + T$ is evident highlighting that the control techniques indeed mitigate inter-component momentum transport. Therefore, in the successful controlled cases, fluctuations remain somewhat restricted to the streamwise velocity component. The corresponding suppressed momentum transfer between the mean flow and the fluctuations is symbolised by turbulent kinetic energy and Reynolds shear stress production decay as shown in Figures 7(a)-(d). According to the Fukagata-Iwamoto-Kasagi identity [64], suppressing the integrated Reynolds shear stress is equivalent to drag reduction. The statistical analysis of the control techniques

emphasises a connection between vorticity fluctuations and drag reduction which overlaps with the findings of previous studies uncovering links between friction drag, enstrophy [47] and velocity-vorticity correlations [65].

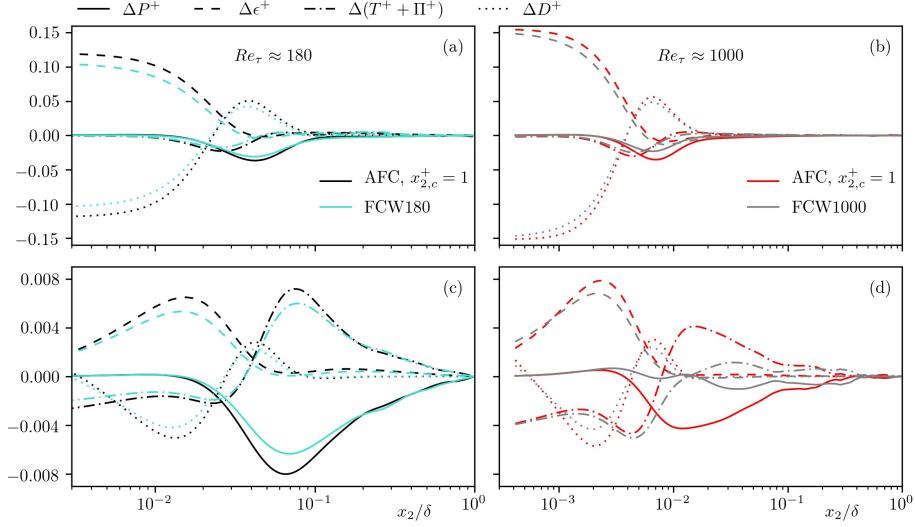


Figure 7: Change in turbulent kinetic energy and Reynolds shear stress transport terms with wall distance for different control techniques at $Re_\tau \approx 180$ (left column) and $Re_\tau \approx 1000$ (right column). Turbulent kinetic energy (a)-(b), and Reynolds shear stresses $-\langle u'_1 u'_2 \rangle$ (c)-(d).

3.4. Lagrangian Wall Motions

Finally, wall motions of the compliant surfaces are analysed to evaluate their realisation potential. To this end, the solely streamwise Lagrangian displacement field of the wall is determined by integrating the velocity field. Considering the mounted rotating disc model in Figure 1(b), the analysed Lagrangian displacement field describes points travelling from one disc to another. For video sequences visualising the wall velocity and the displacement fields, see the [Supplementary Data](#) available online.

The material lines corresponding to SCW180 preserve their consistency and exhibit standing wave-like movements but such wall motions are not sufficient to sustain statistically significant friction drag reduction (see Table 2). By comparison, in the case of FCW180, the wall needs to support large deformations in positive and negative directions within a short distance in order to cancel wall

398 shear stress fluctuations originating from streaks. After the material points are
399 clustered in the neighbourhood of low wall velocity regions between streaks, they
400 travel together. Both FCW1000 and SCW1000 behave similarly to FCW180
401 resulting in dense and sparse wall sections which are difficult to realise beyond
402 the conceptual rotating disc model. Representative rms displacement values for
403 the selected compliant walls are summarised in Table 3.

Table 3: Root-mean-square displacement values corresponding to selected compliant walls after t_{int} time.

| ID | t_{int} | rms displacement |
|---------|---------------------------------------|------------------|
| SCW180 | $2.74\delta/u_\tau = 495\nu/u_\tau^2$ | $30\delta_\nu$ |
| FCW180 | $2.74\delta/u_\tau = 495\nu/u_\tau^2$ | $501\delta_\nu$ |
| SCW1000 | $0.50\delta/u_\tau = 495\nu/u_\tau^2$ | $393\delta_\nu$ |
| FCW1000 | $0.50\delta/u_\tau = 495\nu/u_\tau^2$ | $764\delta_\nu$ |

404 4. Conclusions

405 Active and passive flow control strategies for drag reduction have been in-
406 vestigated by means of direct numerical simulations of canonical channel flows
407 at friction Reynolds numbers of 180 and 1000. The active control technique
408 used herein was proposed by Choi *et al.* [25], and promoted solely stream-
409 wise wall fluctuations driven by the streamwise wall shear stress. The passive
410 control technique comprised a compliant surface based on an array of damped
411 harmonic oscillators that ensured solely streamwise wall fluctuations similar to
412 those of the foregoing active control approach. Our previous studies demon-
413 strated [34, 39, 40] that the foregoing conceptual compliant surface can sustain
414 drag reduction by exploiting behaviour similar to that of active control. Using
415 direct numerical simulation, we have uncovered the corresponding drag reduc-
416 tion mechanism.

417 For detailed analysis, active control techniques were selected, in addition
418 to relatively flexible and stiff compliant surfaces. It has been demonstrated
419 that, when successful, both active and passive control methods reduce span-
420 wise vorticity fluctuations at the wall (and hence the shear between velocity

421 streaks and the wall). By doing so, the control techniques inevitably strengthen
 422 shear between the streaks, leading to increased wall-normal vorticity fluctua-
 423 tions. The former effect seems to be beneficial from the drag reduction point of
 424 view, whereas the second appears to limit control performance. The Reynolds
 425 stress, vorticity, and Reynolds stress transport statistics suggest that reducing
 426 spanwise vorticity fluctuations at the wall effectively lower vorticity fluctuations
 427 and momentum transfer over the majority of the turbulent boundary layer. The
 428 drag reduction mechanisms of the investigated active and passive control meth-
 429 ods differ from established flow control strategies, such as opposition control
 430 [25–28] and spanwise wall oscillations [37, 59]. According to the Lagrangian
 431 displacement field analysis, large-scale wall motions are required to achieve a
 432 modest friction drag reduction.

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 440 Service (<http://www.archer.ac.uk>).

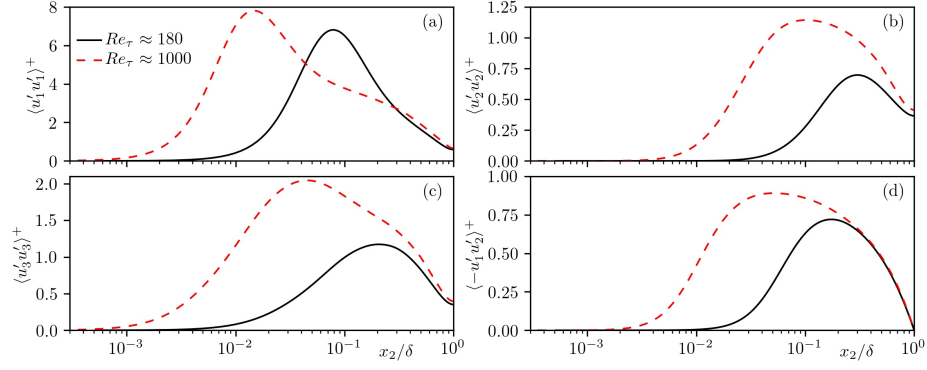


Figure A.8: Reynolds stresses as functions of the wall distance and Reynolds number: stream-wise (a), wall-normal (b), spanwise (c) components, and Reynolds shear stress (d).

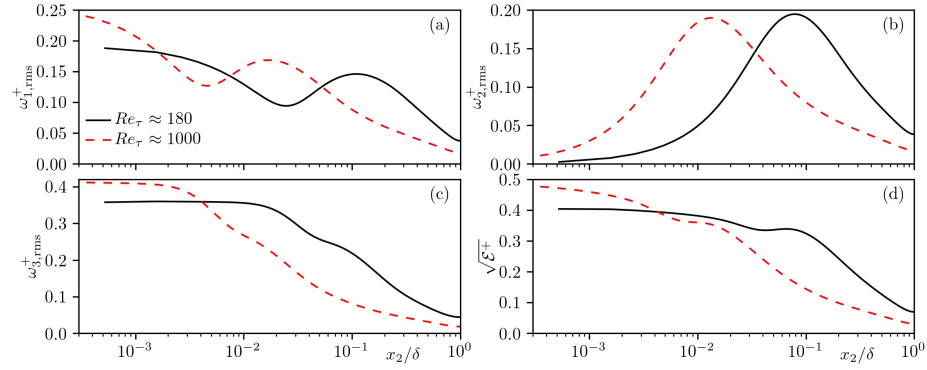


Figure A.9: Vorticity statistics as functions of the wall distance and Reynolds number: stream-wise (a), wall-normal (b), spanwise (c) components, and square root of turbulent enstrophy representing the magnitude of the fluctuating vorticity vector (d).

442 Appendix B. Baseline Reynolds stress transport budgets

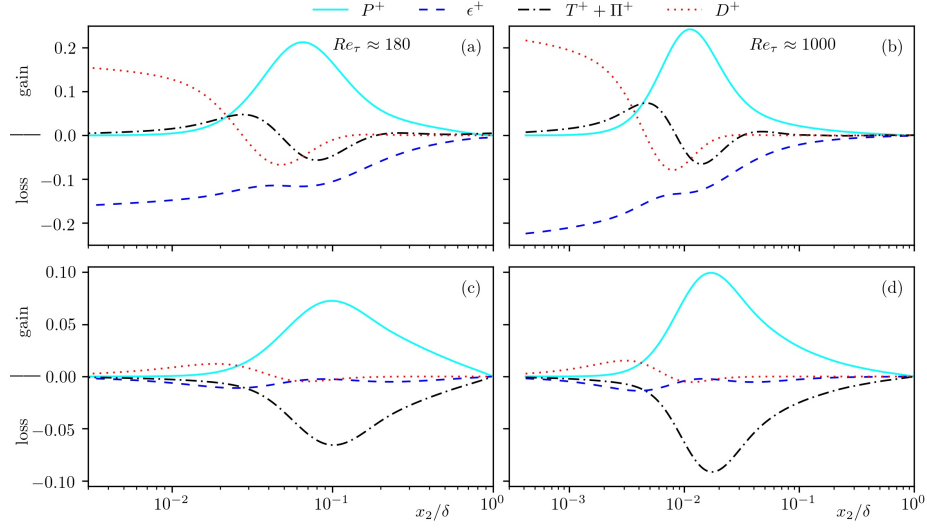


Figure B.10: Turbulent kinetic energy and Reynolds shear stress transport terms as functions of the wall distance at $Re_\tau \approx 180$ (left column) and at $Re_\tau \approx 1000$ (right column): turbulent kinetic energy (a)-(b) and Reynolds shear stress $-\langle u'_1 u'_2 \rangle$ (c)-(d).

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